# 2021

## STATISTICS—GENERAL

Paper: DSE-A-1

(Econometrics)

Full Marks: 50

The questions are of equal value.

The figures in the margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

## 1. Answer any five questions:

 $2 \times 5$ 

- (a) What is BLUE?
- (b) State the assumption required to show the consistency of an OLSE.
- (c) What is the meaning of the term "heteroscedasticity"?
- (d) When does near multicollinearity occur?
- (e) What is the indication of negative residual autocorrelation?
- (f) What will be the impact on standard errors of the regression co-efficients in a regression model if multicollinearity is perfect?
- (g) Suppose Z is an instrument for a regressor X. X is stochastic. To be a valid instrument, what criteria Z must satisfy?
- (h) What does the equation  $\widehat{Y} = \widehat{\beta_0} + \widehat{\beta_1} x$  denote if the regression equation is  $Y = \beta_0 + \beta_1 X_1 + U$ ?

#### 2. Answer any two questions.

 $5\times2$ 

(a) Let the regression results for the impact of per capita GNP (PGNP) and female literacy rate (FLR) on child mortality (CM) be as given below.

$$\widehat{CM}_i^* = 0 \cdot 40 \, PGNP_i^* - 0 \cdot 04 \, FLR_i^*$$

where starred variable indicates standardized variable.

- (i) What are the implications of parameter values?
- (ii) Which regressor has more impact on CM?
- (b) Clearly outline and explain the assumptions of Gaussian Classical Linear Regression models.
- (c) How to deal with the problem of multicollinearity?

#### 3. Answer any three questions.

 $10\times3$ 

(a) Having derived a model for the exchange rate  $S_t$  as a function of the interest rate differential  $r_t$  and performed the following regression

$$S_t = a + br_t + e_t$$

where  $e_t$  is an error term. How would you check for the presence of serial correlation in the error term and how would you deal with it?

- (b) What is an instrument variable? Briefly discuss the Instrumental variable method (single equation model with one explanatory variable)
- (c) In presence of heteroscedasticity in the data, why OLSE of parameters is inappropriate. Give the variance estimator  $\hat{\Sigma}$ , where  $V(\varepsilon) = \Sigma$  and  $Y = X\beta + \varepsilon$ .
- (d) (i) How do you overcome the consequences due to errors in variables?
  - (ii) If  $V(\mathcal{E}) = \Sigma$ , a non-singular, non-diagonal matrix, where  $Y = x\beta + \varepsilon$  is a CLRM and all of the model assumptions hold apart from assumption about  $V(\varepsilon)$ , give the GLSE of  $\beta$ .
- (e) Suppose the model of interest is  $Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \mu_i$ , where  $E(\mu/X) = 0$  and  $E(\mu^2|X) = \sigma^2$  and  $X_1$  and  $X_2$  are uncorrelated in your sample. Will the bivariate regression of Y on  $X_1$  have the same estimate of co-efficient and standard error for  $\widehat{\beta_n}$  as that for multivariate regression of Y on  $X_1$  and  $X_2$ ?